## Mark Scheme (Results)

## Summer 2016

Pearson Edexcel GCE<br>Decision Mathematics 2

6690/01

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## EDEXCEL GCE MATHEMATICS

## General I nstructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of $M$ marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.

## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 1. (a) | e.g. in the practical problem each vertex must be visited at least once. In the classical problem each vertex must be visited just once | B2, 1, $0 \quad$ (2) |
| (b) | $\begin{aligned} & \mathrm{A}-\mathrm{D}-\mathrm{C}-\mathrm{F}-\mathrm{B}-\mathrm{E}-\mathrm{G}-\mathrm{A} \\ & 12+16+19+25+14+41+22=149 \\ & \mathrm{~A}-\mathrm{D}-\mathrm{C}-\mathrm{F}-\mathrm{G}-\mathrm{E}-\mathrm{B}-\mathrm{A} \\ & 12+16+19+25+41+14+31=158 \end{aligned}$ | M1 <br> A1 A1 |
| (c) | $\begin{aligned} & \hline \text { RMST weight }=86 \text { (miles) } \\ & 86+12+15=113 \text { (miles) } \end{aligned}$ | $\begin{aligned} & \hline \text { B1 } \\ & \text { M1 A1 } \\ & \hline \end{aligned}$ |
| (d) | $113 \leq$ optimal distance $\leq 149$ | $\mathrm{B} 2,1,0 \quad \text { (2) }$ $10 \text { marks }$ |
| Notes for Question 1 |  |  |

a1B1: Understands the difference is connected to the number of times each vertex may be visited (but maybe incorrectly attributed). Must be an attempt at a difference (so must refer to both the classical and practical problems explicitly). Technical language (vertex/node) must be correct. Need not imply each/every/all (oe) vertices for this first mark
a2B1: Correctly identifies which is classical and which is practical and correctly states the difference. Must imply that each/every/all (oe) vertices are visited, so for example, 'the practical problem visits a vertex at least once while the classical visits a vertex only once' is B1B0 (note that B0B1 is not possible in (a))
b1M1: Either one correct route, must return to A, or one correct length stated (do not isw in part (b) if correct lengths seen but are then doubled)
b1A1: One correct route, must return to A and corresponding length correct
b2A1: Both routes correct and their corresponding lengths correct
c1B1: CAO for RMST weight (either 86 or $20+16+14+19+17$ ) - maybe implied by later working c1M1: Adding $12+15$ (the two least weighted arcs) to their RMST length (the length of their RMST must be in the interval $66 \leq$ RMST $\leq 106$ ) - this mark maybe implied by the correct value for the lower bound c1A1: CAO - if 113 seen without working then award all 3 marks in (c)
d1B1: Their numbers correctly used, accept any inequalities or any indication of interval from their 113 to their 149 (so 113 - 149 can score this mark). This mark is dependent on two totals seen in (b), however, neither of the two totals need to be correct. Please note that UB $>\mathrm{LB}$ for this mark d2B1: CAO (no follow through on their values) including correct inequalities or equivalent set notation (but condone 113 <optimal distance $\leq 149$ )

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 2. (a) | Saturated arcs: SB, SC, AE, DT, FT | M1 A1 (2) |
| (b) | 59 | B1 (1) |
| (c) | $C_{1}=72, C_{2}=86$ | B1 B1 (2) |
| (d) | SABCFET | B1 (1) |
| (e) | The cut through DT, AE and CF (or DT, AE, BC and SC) has a value 62 <br> Value of the flow is 62 , so by max flow - min cut theorem, flow is maximal | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & 8 \text { marks } \end{aligned}$ |
| Notes for Question 2 |  |  |
| a1M1: All correct - accept one omission and/or one extra arc a1A1: CAO |  |  |
| b1B1: CAO (59) |  |  |
| c1B1: CAO (72) |  |  |
| c2B1: CAO (86) |  |  |
| d1B1: CAO (accept, SA, AB, BC, CF, FE, ET) |  |  |
| e1M1: The arcs of the correct cut stated or a correct cut drawn on their diagram in the answer book - please check carefully for this <br> e1A1: Must have stated the (maximum) flow as 62 and a conclusion based on the max flow min cut theorem - they must use all four words, 'max', 'flow', 'min', 'cut' in their conclusion |  |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| 3. (a) | Since maximising, subtract all elements from some value $\geq 72$ |  |
|  | e.g $\left[\begin{array}{cccc}11 & 22 & 25 & 49 \\ 1 & 10 & 52 & 11 \\ 2 & 23 & 24 & 23 \\ 0 & 4 & 5 & 5\end{array}\right]$ | M1 |
|  | Reduce rows $\left[\begin{array}{cccc}0 & 11 & 14 & 38 \\ 0 & 9 & 51 & 10 \\ 0 & 21 & 22 & 21 \\ 0 & 4 & 5 & 5\end{array}\right]$ and then columns $\left[\begin{array}{cccc}0 & 7 & 9 & 33 \\ 0 & 5 & 46 & 5 \\ 0 & 17 & 17 & 16 \\ 0 & 0 & 0 & 0\end{array}\right]$ | M1 A1 |
|  | $\left[\begin{array}{cccc}0 & 2 & 4 & 28 \\ 0 & 0 & 41 & 0 \\ 0 & 12 & 12 & 11 \\ 5 & 0 & 0 & 0\end{array}\right]$ followed by $\left[\begin{array}{cccc}0 & 0 & 2 & 26 \\ 2 & 0 & 41 & 0 \\ 0 & 10 & 10 & 9 \\ 7 & 0 & 0 & 0\end{array}\right]$ | M1 A1ft <br> M1 A1 |
|  | Optimal allocation is $\mathrm{F}=1, \mathrm{~A}=2, \mathrm{Z}=3, \mathrm{E}=4$ | A1 (8) |
| (b) | $($ Total score is $=$ ) 248 | $\begin{aligned} & \text { B1 } \\ & 9 \text { marks } \\ & \hline \end{aligned}$ |

## Notes for Question 3

a1M1: Subtracting from some value which must be $\geq 72$ or all values made negative and then adding a value which must be $\geq 72$. Condone no more than two errors
a2M1: Reducing rows and then columns - candidates may combine the two stages of converting from a maximum to a minimum problem and row reduction which is acceptable
a1A1: CAO
a3M1: Double covered +e ; one uncovered -e ; and one single covered unchanged. 2 lines to 3 lines needed a2A1ft: Follow through on their previous table - no errors
a4M1: One double covered +e ; one uncovered -e ; and one single covered unchanged. 3 lines needed to 4 lines needed (so getting to the optimal table)
a3A1: CSO on final table (so must have scored all previous marks)
a4A1: CAO - this mark is dependent on all M marks being awarded
b1B1: CAO
SC: Minimising

After row reduction
$\left[\begin{array}{cccc}38 & 27 & 24 & 0 \\ 51 & 42 & 0 & 41 \\ 22 & 1 & 0 & 1 \\ 5 & 1 & 0 & 0\end{array}\right]$ and then after column reduction $\left[\begin{array}{cccc}33 & 26 & 24 & 0 \\ 46 & 41 & 0 & 41 \\ 17 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0\end{array}\right]$
scores M0 M1A1 M0A0 M0A0 A0 B0 (so 2 marks max)



e1M1: Finding 8 shadow costs and all 9 improvement indices or at least 1 negative II found
e1A1: CAO for the shadow costs [Alt: A(0), B(-5), C(-4), D(-23), 1(18), $2(22), 3(23), 4(21)]$ and the 9 positive IIs
e2A1: CSO (for part e) + reason + optimal



## Notes for Question 7

All M marks - must bring optimal result from previous stage into calculations so for the first stage (April) if none of 225, 200, 175 or 550 (the optimal results from May) are used then M0. Ignore extra rows. Condone and credit rows that have been crossed out if they can still be read. Must have right 'ingredients' (storage costs, overhead costs, additional worker cost) at least once per stage (as an example for the six rows in April we must see at least one of these rows having a calculation that has either three or four values). Must have values in two of the three colums (State, Action, Dest). If no working seen then the number stated in the Value column must be correct to imply the correct method has been used
a1M1: First stage (April) completed. At least 6 rows, 'something' in each cell (but see M mark guidance above)
a1A1: Any two states correct (condone extra rows)
a2A1: CAO for first stage. No extra rows
a2M1: Second stage (March) completed. At least 6 rows, something in each cell (see M mark guidance above)
a3A1ft: Any two states correct - ft their * values/their smallest value from previous stage (condone extra rows)
a4A1: CAO for second stage. No extra rows
a3M1: Third stage (February) completed. At least 12 rows, something in each cell (see M mark guidance above)
a5A1ft: Any two states correct - ft their * values/their smallest value from previous stage (condone extra rows)
a6A1: CAO for third stage. No extra rows
a4M1: Fourth stage completed. At least 4 rows, something in each cell (see M mark guidance above) a7A1: CAO (no ft) for fourth stage. No extra rows
a1B1:CAO - but must have scored all previous M marks
a2B1:CAO - condone lack of units - but must have scored all previous M marks
b1M1: $700 \times 19-(5 \times 450+19 \times 200+$ their 1700$)$ or $7250-$ their 1700 . Must have scored at least two $\mathbf{M}$ marks in (a)
b1A1: CAO (condone lack of units) - correct answer with no working can score both marks in this part (but is still dependent on at least two $M$ marks awarded in (a))

